Raman scattering from biased molecular conduction junctions: The electronic background and its temperature

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The existence of background in the surface-enhanced Raman scattering from molecules adsorbed on metal surfaces has been known since the early studies about this phenomenon and is usually attributed to transitions between electronic states of the metal substrate. This paper reformulates the theory of this phenomenon in the framework of the nonequilibrium Green function formalism, which makes it possible to extend it to the case of Raman scattering from nonequilibrium (biased and current-carrying) molecular junctions. Following recent experiments, we address, in particular, the Raman-scattering measurement of current-induced electronic heating. The Raman temperature, defined by fitting the ratio between the Stokes and the anti-Stokes Raman signals to a Boltzmann factor is compared to another measure of electronic heating obtained by assuming that, close to the molecule-metal contact, the electronic distribution is dominated by the transmission process. We find that the Raman temperatures considerably exceed this upper bound to the metal-electron heating. In agreement with this observation, we show that the Raman temperature reflects the electronic nonequilibrium in the molecular bridge itself. We also show that the Raman-temperature concept breaks down at large biases.

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I. INTRODUCTION

Studies of Raman scattering from molecular conduction junctions lie at the juncture of two contemporary fields of research: Molecular electronics, which focuses on the electronic transport properties of molecules connecting between conducting leads and molecular plasmonics, in particular, surface-enhanced Raman scattering (SERS), which exploits the behavior of the electromagnetic field near metallic interfaces to enhance and to control the optical response of molecules adsorbed at such interfaces. Typical configurations of molecule conduction junctions are similar to structures discussed as hot spots in single-molecule SERS,\textsuperscript{1,10} that is, structures characterized by strong enhancement of the local electromagnetic field. Indeed, this enhancement was important for obtaining detectable signals in recent studies of Raman scattering from such junctions.\textsuperscript{11–13} Not surprisingly, it was found that the junction conductivity and the Raman-scattering signal show correlated behavior,\textsuperscript{11} indicating that Raman scattering can probe structural changes in the junction that affects its conductivity.\textsuperscript{14}

Further development of optical methods in the context of molecular conduction junctions is obviously very desirable because interaction with the radiation field can provide new ways of characterization and control of such systems.\textsuperscript{17} Many aspects of optical interaction in tunneling junctions have been studied in the past.\textsuperscript{18} Among these are observations of light emission from current-carrying molecular junctions,\textsuperscript{2,19–33} affecting junction conduction properties and inducing dc currents by optical signals,\textsuperscript{34–40} and using optical pulses to cause conduction switching by affecting structural changes.\textsuperscript{41–51} Relevant to our present discussion are recent demonstrations\textsuperscript{12,13} that it can be used to determine the effective temperature in biased and current-carrying junctions.

This experimental effort has been accompanied by theoretical studies of various phenomena pertaining to what we may call junction spectroscopy. Such studies attempt to characterize the correlation between optical response and electrical conduction properties of molecular conduction junctions,\textsuperscript{52–69} and are supplemented by parallel studies of the behavior of optical fields at metallic interfaces pertaining to such junctions.\textsuperscript{70} Recent papers by us and co-workers have addressed current-induced light and light-induced current phenomena in molecular junctions,\textsuperscript{71–73} as well as the possibility to control the latter by properly shaped photon pulses.\textsuperscript{74,75} Another paper presents a general theory of Raman scattering from molecular conduction junctions,\textsuperscript{76,77} and addresses, among other issues, the possibility to use this phenomenon to determine the junction effective temperature. This paper provides the starting point for the present discussion.

The present paper addresses recent experimental observations\textsuperscript{12} of heating in current-carrying tunneling junctions with and without molecular bridges, using Raman scattering as a probe. The issue of heating in biased molecular junctions has attracted considerable recent experimental and theoretical attention, motivated by the relevance of this phenomenon to current-induced chemical change and to junction stability.\textsuperscript{78,79} This issue was addressed theoretically by several authors,\textsuperscript{80–98} however, the experimental observation of such heating\textsuperscript{12,73,90–105} depends on finding a suitable probe. First attempts to estimate junction heating\textsuperscript{100,101} have used the threshold for bond breaking under tension as such a probe. Raman scattering provides a more direct probe that, in principle, can be applied separately to the different modes by using the information conveyed by the relative intensities of the corresponding Stokes- (S) anti-S (AS) components of scattering signals.\textsuperscript{12,13,76} Indeed, Ward and co-workers\textsuperscript{12} were able not only to assign effective temperatures to several molecular vibrations and to follow its change as a function of bias voltages, but also to address the temperature of the underlying electronic continuum. This observation, in principle, is very significant since standard treatments of
conduction in nanojunctions including molecular junctions usually assume that the metal contacts remain at their original thermal equilibrium. While heating of molecular degrees of freedom was considered by us and others in previous theoretical papers, this observation makes it necessary to address electronic heating of contacts as well.

Focusing on this issue, several questions should be considered. First, using Raman scattering as a temperature probe of current-induced heating has the drawback that the incident light itself can heat the system. Indeed, Ward and co-workers find temperature rise associated with junction illumination at zero bias. In the present paper, we focus on the additional heating associated with electronic conduction in the biased junction. Second, bias-induced heating is also observed in pure metallic junctions that do not incorporate bridging molecules. Here, we focus on molecular junctions characterized by relatively low transmission where direct charge transfer between metal electrodes can be disregarded. Next, one may question why electronic conduction through the molecular bridge affects heating of electrons in the macroscopic electrodes. The answer is that the molecular current creates a region in the metal, near the metal-molecule contact, where the electronic distribution is out of equilibrium. Because of the fast (10–100 fs) relaxation of electrons in metals, this region is very small (a rough estimate based on the Fermi velocity yields ~10 nm for its linear size), however, Raman scattering, dominated by the molecule-radiation field interaction and affected by the molecule-metal interaction, probes exactly this nonequilibrium region. Finally, a general problem in describing heating in nonequilibrium systems is the natural desire to describe such heating in terms of a single parameter, an effective temperature. Often, as has been pointed out, this may provide a qualitative indication of heating, but different definitions may yield different numerical values for such temperatures. These considerations are reflected in the theory forwarded below.

The analysis of electronic heating in Raman-scattering experiments is closely related to the general discussion of the continuous background observed in the SERS experiment, see, e.g., Refs. 107–111. Although different origins of this phenomenon were postulated over the years, there seems to be general agreement that this contribution to the Raman signal (that is, inelastic light scattering) involves excitation of electron-hole pairs in the metal. What makes it difficult to identify a unique mechanism for this phenomenon is that more than one process may be involved. In particular, the observed background often result from both Raman and fluorescence processes, the latter involving intermediate loss of coherence by dephasing or thermal relaxation. Furthermore, in studies involving metal particles, the fluorescence appears to emanate from plasmon excitations in these particles, suggesting the possibility that plasmons are formed by relaxation of e-h pairs. Although our view is somewhat different, the relative contribution of Raman and fluorescence processes to the observed inelastic continuum is an important attribute of the process.

Whatever the detailed mechanism(s) of the background scattering/emission is, a corresponding theory will depend on the electronic distribution in the metal substrate, which, for bias-driven junctions, should reflect its nonequilibrium character. In the present paper, we describe such a theory, using the non-equilibrium Green function (NEGF) technique. Our model is similar to those used earlier for this problem, however, the NEGF methodology makes it possible to generalize these treatments for the nonequilibrium situations that characterize biased molecular junctions. Furthermore, we advance a simple theoretical description of the nonequilibrium electronic distributions at the two metal contacts of the biased junction and use it to estimate the junction heating and the associated electronic Raman spectrum. Our results compare well with the observations of Ref. 12 for reasonable choices of junction parameters, however, they also emphasize the difficulties inherent in the use of the effective-temperature concept. Furthermore, they place the origin of the observed electronic heating more with the electronic-nonequilibrium distribution in the molecular bridge than with that in the metal. A short account focusing on this issue recently was published.

Our theory of the electronic Raman background in biased molecular junctions is presented in the next section. Irrespective of our later focus on junction heating, this theory makes interesting and testable predictions concerning the bias voltage dependence of this spectrum. In Sec. III, we present a simple description of the nonequilibrium electronic distribution at the metal-molecule contact and use it to define a voltage-dependent effective temperature. The voltage-dependent electronic Raman scattering and the effective temperature associated with its AS component are discussed in Sec. IV in comparison with the experimental results of Ref. 12. Section V concludes.

II. ELECTRONIC RAMAN SCATTERING IN BIASED MOLECULAR JUNCTIONS

We consider a molecular junction driven by a single-mode cw light under current-carrying conditions. The junction consists of a molecule \( M \) coupled to two metal contacts \( L \) and \( R \), considered to be free-electron carriers (Fermi seas) each at its own thermal equilibrium characterized by electrochemical potentials \( \mu_L \) and \( \mu_R \), respectively. The molecule is represented by a two-level (highest occupied molecular orbital-lowest unoccupied molecular orbital) model used in our previous paper (Fig. 1). We only focus on the contribution to the Raman signal (that is, inelastic

![FIG. 1. A two-level model for a molecular conduction junction.](image-url)
light scattering) associated with energy imparted to electronic states in the metals and, therefore, for simplicity, omit molecular vibrations from our consideration. The electronic inelastic spectrum dresses the Raleigh-scattering signal in the calculation discussed below, and it similarly dresses any vibrationally inelastic signal in a calculation that incorporates vibrational motion. The Hamiltonian of the system is

\[ \hat{H} = \hat{H}_M + \sum_{K=L,R} (\hat{H}_K + \hat{V}_{KM}) + \hat{H}_{\text{opt}} + \hat{V}_{\text{opt},M}. \]  

(1)

where \( \hat{H}_M \) is the molecular Hamiltonian, \( \hat{H}_K (K = L,R) \) are the Hamiltonians of the metal electrodes, and \( \hat{V}_{KM} \) are the corresponding couplings that represent electron transfer between molecule and electrode. \( \hat{H}_{\text{opt}} \) is the Hamiltonian of the radiation field, and \( \hat{V}_{\text{opt},M} \) is the molecule-radiation-field coupling.

\[ \hat{H}_M = \sum_{m=1,2} \epsilon_m \hat{a}^\dagger_m \hat{a}_m, \]  

(2)

\[ \hat{H}_K = \sum_{k,K} \epsilon_k \hat{c}^\dagger_k \hat{c}_k, \]  

(3)

\[ \hat{V}_{KM} = \sum_{m=1,2,k,K} (V_{km} \hat{c}^\dagger_k \hat{a}_m + \text{H.c.}), \]  

(4)

\[ \hat{H}_{\text{opt}} = \sum_a \hbar \nu_a \hat{a}^\dagger_a \hat{a}_a, \]  

(5)

\[ \hat{V}_{\text{opt},M} = \sum_a (U_a \hat{a}^\dagger_a \hat{a}^\dagger_1 + \text{H.c.}). \]  

(6)

Here, \( \hat{a}^\dagger_m (\hat{a}_m) \) and \( \hat{c}^\dagger_k (\hat{c}_k) \) are creation (annihilation) operators of electrons in state \( m \) on the molecule and state \( k \) in the contact, respectively, and \( \hat{a}^\dagger_a (\hat{a}_a) \) are creation (annihilation) operators of photons in optical mode \( \alpha \).

The calculation of Raman scattering is facilitated by distinguishing between the incoming (or pumping) mode \( i \) and the set of final (or accepting) modes \( \{ f \} \) of the radiation field. The former is assumed to be populated by one photon, and only processes of in-scattering from this mode into the system are considered (that is, backaction of the molecule onto this mode is disregarded). The latter are empty modes of the field: Population flux into these modes is monitored by the measuring device, but they do not act back on the system, i.e., only out-scattering from the system into these modes is taken into account.

In Refs. 76 and 77, we have distinguished between normal and inverse Raman processes according to whether the molecule is initially in the ground or in the excited state. The latter occurrence is possible in a strongly biased junction. Here, we only consider normal Raman processes. The corresponding expression for the flux from the incoming mode \( i \) to the outgoing mode \( f \) representing light scattering from the molecular junction at steady state was obtained in Ref. 77 [see Eq. (28) there].

\[ J_{i \rightarrow f}^{(\text{sr})} = \frac{|U_i|^2 |U_f|^2}{\hbar^4} \int_{-\infty}^{+\infty} d(t - \tau) \int_{-\infty}^{+\infty} dt_1 \int_{-\infty}^{+\infty} dt_2 \]  

\[ \times e^{i \nu f (t - \tau)} e^{-i \nu (t_1 - t_2)} \langle \hat{D}(t_2) \hat{D}(t) \hat{D}(t_1) \hat{D}(1) \rangle, \]  

(7)

where \( \hat{D} = \hat{a}^\dagger_1 \hat{a}^\dagger_2 \) \( (\hat{D} = \hat{a}^\dagger a) \) is the molecular deexcitation operator. Note that generalized Franck-Condon factors that appear in Eq. (28) of Ref. 77 are omitted in Eq. (7) since we do not consider vibrational transitions.

Equation (7) is already of the lowest needed (fourth) order in the molecule-radiation-field interaction, so for this order, this interaction is disregarded in evaluating the four-time correlation function in the integrand. Substituting Eq. (8) into Eq. (7), applying Wick’s theorem, \(^{119}\) and assuming that energy separation between the two molecular levels is much larger than their broadening due to hybridization with a metal state (this makes it possible to disregard nondiagonal elements of the single-electron Green function that describes the molecule in the junction) leads to (see the Appendix for more details)

\[ J_{i \rightarrow f} = \frac{2\pi}{\hbar} |U_i|^2 |U_f|^2 \rho(\nu_i) \rho(\nu_f) \delta(h\nu_i - h\nu_f) \]  

\[ \times \left\langle \int \frac{dE}{2\pi} \int \frac{dE}{2\pi} G^\dagger (E_j^i) G_j^i G^\dagger (E_j^f) G_j^f \right\rangle \]  

\[ \times \left\langle \sum_{m=1,2} \frac{\delta(h\nu_i - E_1^m - E_2^m + i\delta)}{h\nu_i + E_1^m - E_2^m + i\delta} \right\rangle \]  

(9a)

\[ + \left\langle \int \frac{dE}{2\pi} \int \frac{dE}{2\pi} \delta(h\nu_i - E_1^i - h\nu_f - E_2^f) \right\rangle \times G^\dagger (E_j^i) G_j^i G^\dagger (E_j^f) G_j^f \]  

(9b)

\[ + \left\langle \int \frac{dE}{2\pi} \int \frac{dE}{2\pi} \delta(h\nu_i + E_1^i - E_2^f + i\delta) \right\rangle \times G^\dagger (E_j^i) G_j^i G^\dagger (E_j^f) G_j^f \]  

(9c)

\[ + \left\langle \int \frac{dE}{2\pi} \int \frac{dE}{2\pi} \int \frac{dE}{2\pi} \int \frac{dE}{2\pi} \delta(h\nu_i + E_1^i + E_2^f - h\nu_f - E_2^f) \right\rangle \times G^\dagger (E_j^i) G_j^i G^\dagger (E_j^f) G_j^f \]  

(9d)

\[ \times \left\langle \frac{\delta(h\nu_i + E_1^i - E_2^f + i\delta)}{h\nu_i + E_1^i - E_2^f + i\delta} \right\rangle, \]  

(9e)

where \( G^\dagger (E_j^m) (m = 1,2) \) are greater and lesser projections of the single-particle Green function,

\[ G^\dagger (E) = i \sum_{K=L,R} \frac{\Gamma^K_m [1 - f_K(E)]}{(E - \epsilon_m)^2 + (\Gamma^K_m)^2}, \]  

(10)

\[ G^\dagger (E) = i \sum_{K=L,R} \frac{\Gamma^K_m f_K(E)}{(E - \epsilon_m)^2 + (\Gamma^K_m)^2}, \]  

(11)
and where

$$\Gamma^K_m(E) \equiv 2\pi \sum_{k \in K} |V_{km}|^2 \delta(E - \varepsilon_k) \quad (K = L, R)$$  \hspace{1cm} (12)$$

are electron escape rates from molecular level $m$ into contact $K$, and $\Gamma^m \equiv \sum_{K=L,R} \Gamma^K_m$. In general, the parameter $\delta$ should be replaced by broadening of the optical signal due to interaction with the environment. The latter is not included in the model explicitly, i.e., within the model $\delta \to 0 \pm$. The notation used for the integration variables in Eqs. (9) is chosen to help the physical interpretation of the different contributions to the scattering signal: We use the upper indices (1) or (2) to mark the molecular origin (molecular states 1 or 2) of the electronic optical transitions (in our model, electrons interact with light through their interaction with the molecule), whereas, lower indices $i$ and $f$ mark initial and final states of the scattering process.

The scattering flux (9) is seen to include four contributions: Rayleigh scattering, Eq. (9a), and three types of electronic Raman-scattering processes, Eqs. (9b)–(9d). In the following, we are interested in Raman scattering only. Equations (9b) and (9c) represent electronic Raman scattering with initial and final metal electronic states near the ground ($m = 1$) and excited ($m = 2$) states of the molecule, respectively. Equation (9d) corresponds to a coherent two-electron Raman-scattering event with electrons starting in both ground and excited states of the molecule. The processes are sketched in Fig. 2. The Fermi occupations involved in these expressions imply that, at zero bias and low-temperature processes, (b) or (c) dominate if level 1 or 2, respectively, is closer to the Fermi energy, whereas, process (d) can contribute only weakly since it requires that both levels 1 and 2 couple to occupied and nonoccupied metal states. For highly biased junctions, all processes can contribute as will be seen below.

III. HEATING OF THE ELECTRONIC DISTRIBUTION

Standard theories of molecular conduction are based on the Landauer theory that assumes that electrons entering the junction reflect the Fermi distribution of their reservoir of origin. At the same time, Landauer theory assumes that thermal relaxation of the transmitted charge takes place only in the interior of the electrode. Obviously, in a current-carrying junction, a small region near the metal-molecule contact will be characterized by different distributions for the electrons moving toward the junction and away from it. The electronic distribution as a function of energy and position in this region depends on the relaxation processes associated with electron-electron and electron-phonon interactions. A simple model that addresses this issue was discussed in Ref. 86. Here, we assume that the electronic distribution in the electrodes’ contact regions that contribute to the inelastic light-scattering signal through their interaction with the molecular bridge is dominated by the transmission process and that thermal relaxation can be disregarded in these regions. Obviously, a heating estimate based on this assumption is an upper bound to the actual heating. Denoting the junction transmission coefficient by $T(E)$ and the equilibrium Fermi distributions in the left and right electrodes by $f_K(E)$, $K = L, R$, the steady-state electronic distributions in these contact regions are

$$f^{SS}_L(E) = \frac{1}{2} \{f_L(E) + [1 - T(E)] f_L(E) + T(E) f_R(E)\} \quad = f_L(E) + \frac{1}{2} T(E) [f_R(E) - f_L(E)]. \quad (13a)$$

$$f^{SS}_R(E) = f_R(E) + \frac{1}{2} T(E) f_L(E) - f_R(E). \quad (13b)$$

It is a common practice to associate an effective temperature with a given nonequilibrium distribution. Usually, it is performed by fitting the distribution to the corresponding equilibrium expression, that is, using Eq. (13) to define effective temperatures according to

$$f^{SS}_K(E) = \frac{1}{e^{\frac{1}{4}(E - \mu_K)/kT_K^m} + 1}, \quad K = L, R. \quad (14)$$

However, this procedure is inadequate since the distributions (13) can be very different from a Fermi function. Instead, we define the effective temperature by the requirement that a weak contact between our nonequilibrium system and an

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FIG. 2. (Color online) Sketch of electronic-scattering events corresponding to expressions in Eq. (9). Shown are (a) Rayleigh and (b)–(d) three types of electronic Raman-scattering events. In (a), the light-scattering process may be accompanied by an electron that goes from a state of energy $E^{(1)}$ to a state of energy $E^{(2)}$ then returns to the same state $E^{(1)}$, which involves twice the Fermi factors $f(E^{(1)})[1 - f(E^{(2)})]$ as seen in Eq. (9a). In (b), the scattering process is accompanied by an electron starting from a state of energy $E^{(1)}$ and ending in state $E^{(1)}$ [hence, the appearance of the Fermi product $f(E^{(1)})[1 - f(E^{(1)})]$ in Eq. (9b)], having gone through an intermediate state of energy $E^{(2)}$, which can contribute if empty (implying the square of the corresponding Fermi factor $[1 - f(E^{(2)})]^2$). In (c), the inelastic contribution results from an electron going from a state of energy $E^{(1)}$ to energy $E^{(2)}$ while another electron goes from energy $E^{(2)}$ to fill back the hole formed in $E^{(1)}$. This involves the occupation probability product $f(E^{(1)})^2 [1 - f(E^{(1)})]$, having been through an intermediate state of energy $E^{(2)}$. Finally, process (d) results from two independent electronic transitions: The destruction of the incoming photon is accompanied by an electron moving from $E^{(1)}$ to $E^{(2)}$ while the creation of the outgoing photon is accompanied by an electron going from state $E^{(2)}$ to state $E^{(1)}$.
equilibrium system characterized by the desired effective temperature and the same electrochemical potential ($\mu_L$ or $\mu_R$) carries no heat current. This implies the following definition of the effective temperature:

$$\int \frac{dE}{2\pi} (E - \mu_K) [f_K^{S\Sigma}(E) - f_K(E, T_{\text{eff}})] = 0. \quad (15)$$

For energy-independent transmission, the distributions (13) are characterized by excess holes below the Fermi energy of the lower-voltage side and excess electrons above the Fermi energy on the higher-voltage side, and both amount to heating, i.e., $T_{\text{eff}}^K > T$. It should be emphasized, however, that the nonequilibrium junction really cannot be characterized by a single effective temperature. For energy-dependent transmission, heating is not the same on both sides, and, in fact, can become cooling on one side. This limitation of the effective-temperature concept also will become evident in the next section when we compare the effective temperature obtained from the electronic contribution to inelastic light scattering to that associated with Eqs. (13).

IV. RESULTS: THE RAMAN CONTINUUM AND ITS EFFECTIVE TEMPERATURE IN BIASED MOLECULAR CONDUCTION JUNCTIONS

In what follows, we present results of model calculations of the Raman continuum in equilibrium and in biased molecular conduction junctions, evaluate the heating associated with the current flow through the biased junction, and compare the effective temperature extracted from the light-scattering signal to that associated with the nonequilibrium distributions (13). Unless otherwise stated, we have used the junction model described in Sec. II and Fig. 1 with the following set of parameters: The Fermi energy (electrochemical potential) in the unbiased junction is taken as zero, and the molecular levels are placed at $E_1 = -1.5$ and $1.0$ eV. The potential bias $V_{sd}$ is assumed to divide symmetrically between the two contacts, so the electrochemical potentials under bias are $\mu_L = |e|V_{sd}/2$ and $\mu_R = -|e|V_{sd}/2$ ($e$ is the electronic charge). The incident frequency is taken as $\hbar\nu_i = 1.5$ eV. The molecule-metal coupling is measured by the widths $\Gamma_m^K$; $m = 1, 2, K = L, R$. These four parameters are all taken to be $0.25$ eV in a symmetric junction. We also have examined junction asymmetry, e.g., when one of the leads is an STM tip, taking, in this case, $\Gamma_m^L = 0.25$ and $\Gamma_m^R = 0.0025$ eV for both molecular levels. The width parameter $\delta$ in Eq. (9) should reflect environmental broadening and is taken as $0.01$ eV. Finally, we examine the system behavior at two temperatures $T = 0, 300$ K. All energy integrations are performed on a grid of $3001$ points distributed uniformly in the interval $-3.0 \cdots 3.0$ eV.

Figure 3 shows the effective electronic temperatures calculated from Eq. (15) with these model parameters. Figures 3(a) and 3(b) show results for the symmetric $\Gamma^L = \Gamma^R$ and asymmetric $\Gamma^L \neq \Gamma^R$ junctions as detailed above, and Fig. 3(c) shows results obtained from a junction characterized by a single effective temperature: $T_{\text{eff}}^L = T_{\text{eff}}^R = T_{\text{eff}}$. The inset shows the corresponding $I/V$ curves, for which the $T = 0$ and $T = 300$ K results overlap. (b) Same results for the asymmetric junction case. (c) Similar results for a tunneling junction characterized by a square barrier of height $5$ eV (above the Fermi energy of the unbiased junction) and width $3$ Å.

FIG. 3. (Color online) (a) The effective temperatures, Eq. (15), calculated for symmetric junctions with ambient temperatures $T = 0$ and $300$ K. The blue full and dashed lines, respectively, show the left and right electronic temperatures for the case $T = 0$ K. The red dotted and dashed-dotted lines are similar results for $T = 300$ K. The inset shows the corresponding $I/V$ curves, for which the $T = 0$ and $T = 300$ K results overlap. (b) Same results for the asymmetric junction case. (c) Similar results for a tunneling junction characterized by a square barrier of height $5$ eV (above the Fermi energy of the unbiased junction) and width $3$ Å.
This is not seen in the corresponding panels of Figs. 4(a). This is not seen in the corresponding panels of Figs. 4(a). In this case, the effective temperature associated to Eqs. (9)–(11) and (16) is found to be in excellent agreement with the electronic Raman scattering becomes meaningless. We return to this issue below.

The results shown in Fig. 4 emphasize the importance of the relative positions of the relevant molecular levels with respect to the left and right chemical potentials in determining the light-scattering signal as a function of the frequency shift and bias. This also is seen in Fig. 5 where the Raman signal is displayed against the bias potential. We see again that the electronic inelastic light scattering is dominated by different contributions at low and high biases and that the AS signal can exceed the S signal at high bias.

As in the Raman shift, plots shown in Fig. 4, also the voltage dependence depicted in Fig. 5, mainly reflects the strong energy dependence of the Fermi functions appearing in Eqs. (9)–(11). This sensitivity suggests that attempts to characterize the junction temperature from the S and AS signals should be regarded with caution. This is made evident by comparing Figs. 6 and 3. Figure 6 depicts the Raman effective temperature, and this indeed is satisfied approximately for all cases displayed in Fig. 6 except for the asymmetric junction cases displayed in Fig. 6 except for the asymmetric junction.

FIG. 4. (Color online) (a) The electronic Raman intensity, $J_{\nu_i\rightarrow\nu_f} \sim J_{\nu\rightarrow\nu} v_f^3$, calculated for the symmetric junction, $\Gamma_L^f = \Gamma_R^f = 0.25$, $m = 1, 2$, displayed as a function of the Raman shift $\nu_i - \nu_f$ for $V_{sd} = 0$ (left panels) and $V_{sd} = 2$ V (right panels) and for ambient temperatures $T = 0$ K (upper panels) and $T = 300$ K (lower panels). The solid (red) line shows the overall light-scattering intensity, whereas, the other lines correspond to the different contributions: Eqs. (9b) (dashed, blue), (9c) (dotted, black), and (9d) (dashed-dotted, magenta). (b) Same as (a), for the asymmetric junction, $\Gamma_L^f = 0.25$ eV, $\Gamma_R^f = 0.0025$ eV, and $m = 1, 2$.

Figure 4 shows the electronic contribution to the inelastic light-scattering signal calculated for our model. Several observations are noteworthy: First, the equilibrium (zero-bias) signal is dominated by the contribution (9c) because the upper molecular level 2 lies closer to the Fermi energy than the lower level 1. [From Eqs. (9b) and (9c), it follows that the relative magnitudes of these terms go like $(1 - f_j)(1 - f_2)$ and $f_1 f_2$, respectively]. When the bias increases, the electrochemical potential of the left lead approaches level 2, and, more importantly, that of the right lead comes closer to level 1, whereas, contributions (9b) and (9d) that require finite-hole population near level 1 also become important. For high enough bias, contribution (9d), which requires partially populated metal electronic states near both levels 1 and 2, can become the most significant, as seen in the right panels of Fig. 4(a). This is not seen in the corresponding panels of the asymmetric case, Fig. 4(b) because, although level 1 is approached by the electrochemical potential of the right lead, the corresponding hole population near this level essentially is unaffected because of the very weak right electrode-molecule coupling. Second, when process (9d) becomes important, the AS signal may exceed the S intensity as seen in the right panels of Fig. 4(a). In this case, the effective temperature associated with the electronic Raman scattering becomes meaningless. We return to this issue below.

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$$T_{S/AS}^\text{eff} = \frac{\Delta \nu}{\ln \left( \frac{f_{\nu_i - \nu_f + \Delta \nu}^f f_{\nu_i - \nu_f + \Delta \nu}^r}{f_{\nu_i - \nu_f - \Delta \nu}^f f_{\nu_i - \nu_f - \Delta \nu}^r} \times \frac{(\nu_f + \Delta \nu)^3}{(\nu_f - \Delta \nu)^3} \right)},$$

and is plotted against the Raman shift. Independence of $T_{S/AS}^\text{eff}$ on the Raman shift is a prerequisite for a meaningful effective temperature, and this indeed is satisfied approximately for all cases displayed in Fig. 6 except for the asymmetric junction at low ambient temperatures. As pointed out above, this apparently simple picture breaks down at higher voltages where the S/AS ratio can become smaller than 1 and using Eq. (16) for a temperature estimate is unfeasible. It should be emphasized that the Raman temperature calculated according to Eqs. (9)–(11) and (16) is found to be in excellent agreement.
panels correspond to ambient temperatures as defined by the choice of the $\Gamma_1$ parameters. Upper and lower panels show results for the symmetric and asymmetric junctions as a function of the inelastic shift for different voltage biases. Left and right panels correspond to ambient temperatures $T = 0$ and $T = 300$ K, respectively.

with the imposed ambient temperature at equilibrium. However, at least for high bias, the information embedded in the inelastic scattering continuum cannot be described by a useful Raman effective temperature, although it certainly shows evidence of electronic heating in the biased junction.

Even in the low-voltage regime shown in Fig. 6, the temperatures estimated from Eq. (16) were significantly higher than those obtained directly from the steady-state electronic distribution, Eq. (15), which was argued above to constitute an upper bound to the actual heating. The fact that the Raman temperature implies heating that is considerably larger than what can be associated directly with the electronic distribution in the molecule suggests that its origin lies elsewhere.

We have considered this origin in a recent short paper. An important feature of our model is the assumption that the interaction between the junction and the radiation field that give rise to the Raman scattering originates from that between the molecular bridge and the radiation field. This implies that, although the Raman signal discussed here is associated with electronic transitions in the metal, the coupling to the radiation field results from the metal-molecule interaction; therefore, the calculated scattering may be affected by the electronic nonequilibrium in the molecule.

To examine the possible significance of this effect, we have attempted to estimate the effective electronic temperature $T_M$ of the nonequilibrium molecule in two ways. One (already presented in our recent paper) uses an analog of Eq. (15),

$$\int \frac{dE}{2\pi} G_m^\ast(E) = \frac{dE}{2\pi} \sum_{m=1,2} \{ f(E, \mu_M, T_M) G_m^\ast(E) \} + [1 - f(E, \mu_M, T_M)] G_m^\ast(E) = 0, \quad (17)$$

which represents the condition that the heat current between the molecule and a fictitious equilibrium free-electron bath, characterized by the same chemical potential $\mu_M$ and the effective temperature $T_M$, vanishes. Although the physics behind Eq. (17) is clear, its weakness lies in the fact that the chemical potential $\mu_M$ is not well defined. As in Ref. 117, we use a heuristic extension of the equilibrium expression $\mu = (eV / \hbar n)$ to obtain, for a steady state characterized by given electron and energy fluxes, $J_E$ and $J_r$, respectively, $\mu_M = \frac{dE}{dn} = J_E / J_r$, where $n$ is the number of electrons in the molecule. Both $J_E$ and $J_r$ are easily obtained from the Landauer theory.

Alternatively, effective electronic temperature and chemical potential can be defined as the temperature and the chemical potential of an equilibrium Fermi bath coupled to the nonequilibrium molecule, determined such that both particle and energy fluxes between them vanish

$$\int \frac{dE}{2\pi} \sum_{m=1,2} \{ f(E, \mu_M, T_M) G_m^\ast(E) \} + [1 - f(E, \mu_M, T_M)] G_m^\ast(E) = 0, \quad (18a)$$

$$\int \frac{dE}{2\pi} \sum_{m=1,2} \{ f(E, \mu_M, T_M) G_m^\ast(E) \} + [1 - f(E, \mu_M, T_M)] G_m^\ast(E) = 0. \quad (18b)$$

Equations (18) were solved for the unknowns $T_M$ and $\mu_M$ by an iterative procedure.

Figure 7 shows the results of these calculations. The Raman temperature, Eq. (16), is compared to the effective electronic temperatures of the two leads, obtained from Eq. (15) and to the molecular effective electronic temperatures calculated from Eqs. (17) and (18). Note that Sec. III implies that the Raman temperature should be calculated using the nonequilibrium distributions (13), however, the low-bias results are almost indistinguishable from those obtained using the equilibrium Fermi-Dirac distributions. In fact, for the symmetric junction $\Gamma^L = \Gamma^R$, the results are identical for any bias. To see this, note that the lesser and greater Green functions that enter in the Raman signal have the forms $G^\ast(E) = i[G'(E)]^2 [\Gamma^L f_L(E) + \Gamma^R f_R(E)]; \quad G^\ast(E) = -i[G'(E)]^2 [\Gamma^L [1 - f_L(E)] + \Gamma^R [1 - f_R(E)]], \quad \text{which, for } \Gamma^L = \Gamma^R,$ are not sensitive to the difference between $f_{K}^{eq}(E)$ and $f_{K}^{eq}(K = L, R)$.

While all steady-state temperature estimates shown in Fig. 7 indicate heating, the molecular electronic temperature is seen to be considerably higher than the effective temperature that characterizes the electronic distributions in the leads at the leads-molecule interfaces. The most significant observation is that the Raman electronic temperature is also considerably higher than that of the metal leads and seems to reflect the behavior of the molecular electronic distribution. In the symmetric junction case, the Raman and the molecular estimates are seen to be quite close for both definitions of the latter, Eqs. (17) and (18). For the asymmetric junction, agreement is considerably worse, however, the Raman temperature is bound by the two molecular estimates. More than anything, these estimates show that there is no unique reliable way to define effective temperature in the nonequilibrium system. Still, both estimates of the molecular electronic temperature are...
considerably higher than the effective electronic temperature of the metals and are closer to the Raman temperature. The Raman measure, of course, is unique and well defined, but apart from giving a general indication of heating, it does not quantitatively reflect the actual heating in the metal. Obviously, the observed Raman electronic temperature cannot be taken as a direct estimate of the leads heating.

V. SUMMARY AND CONCLUSIONS

In this paper, we have advanced an approach for the description of the electronic background continuum in Raman scattering from molecules adsorbed on metal surfaces. This approach, based on the NEGF technique, makes it possible to generalize the theory to nonequilibrium situations, and we have applied it to discuss the background Raman scattering from molecular conduction junctions. We obtained (under the simplification that focused on the vibrationless part of the Raman spectrum) an explicit expression, Eq. (9), for the electronic Raman background in terms of the nonequilibrium electronic distributions in the leads. These distributions, Eqs. (13), were obtained from scattering theory considerations under the assumption that electronic relaxation can be disregarded in the contact regions that contribute to the electronic Raman signal. Using together the theory of the Raman background and our estimate for the nonequilibrium electronic distribution at the metal-molecule contact, we were able to analyze nonequilibrium effects in the junction Raman scattering.

As a particular application of our theory, we have considered the heating caused by electronic conduction through the junction. This heating can be monitored through the ratio between the S and the AS Raman signals. Standard theories of molecular conduction junctions assume that the metal leads maintain their equilibrium temperature in the conducting steady state of a biased junction, however, recent experimental results suggest that heating of the electronic distribution near the molecule-metal contact does take place. Our results indicate that: (a) The electronic Raman scattering, namely, the Raman continuous background, indeed contains information about electronic heating in the metal-molecule contact region. (b) The Raman temperature is considerably higher than an upper bound estimated from the (generally energy-dependent) junction transmission coefficient. (c) The Raman temperature reflects the nonequilibrium nature of the molecular bridge more than that of the electronic distributions in the leads. (d) Although the nonequilibrium Raman scattering signal always can be calculated from Eq. (9), the Raman temperature, Eq. (16), becomes meaningless at high bias, when the AS signal may surpass the S one.

In conclusion, recent experimental work has shown that Raman scattering can be a very useful probe of nonequilibrium molecular conduction junctions, however, theoretical analysis is necessary for the correct interpretation of observations and their significance.

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APPENDIX: DERIVATION OF EQ. (9)

Using Eq. (8) in the expression for the Raman flux, Eq. (7), one gets a multitime correlation function of the form \( \langle \hat{d}_1^{\dag}(t_2)\hat{d}_2^{\dag}(t_2)\hat{d}_2^{\dag}(t')\hat{d}_1(t')\hat{d}_1^{\dag}(t)\hat{d}_2(t)\hat{d}_2^{\dag}(t_1)\hat{d}_1(t_1) \rangle \). Here, the time evolution is governed by the junction Hamiltonian \( \hat{H}_M + \hat{H}_K + \hat{V}_{M} \), Eqs. (2)–(4), so the Wicks theorem can be used. Assuming that the separation between molecular levels 1 and 2 is much larger than their broadening, i.e., neglecting interlevel correlations associated with the molecule-metal interaction,
where $G_m^\langle (t - t') = \left< \hat{d}_m(t) \hat{d}_m(t') \right>$ and $G_m^\rangle (t - t') = \left< \hat{d}_m(t) \hat{d}_m(t') \right> (m = 1, 2)$. Equations (10) and (11) are the Fourier transforms of these correlation functions. Using Eq. (A1) in Eq. (7) and expressing all correlation functions in terms of their Fourier transforms leads to the four terms of Eq. (9).
Considerations of coupling magnitudes imply that energy transfer from individual electron-hole pair excitations is an unlikely event. This does not preclude the notion that radiative emission from those transitions is enhanced relative to other types of non-radiative decay of the plasmon. The fact that molecule-induced effect dominates can be seen by comparing Figs. 4(a) and 4(d) of Ref. 12, which show that the molecular junction that carries a current of ∼2 mA exceeds that of a bare junction with ten times larger current. The observed enhancement is likely due to the molecule’s ability to trap and transfer energy to the plasmonic system. This phenomenon has been observed in a variety of systems, including metallic nanoparticles and carbon nanotubes, and has been attributed to the molecule’s ability to enhance the local electric field at the plasmonic surface.

The molecule-induced effect is particularly pronounced in systems where the molecule is strongly coupled to the plasmonic structure. This coupling can be achieved through a variety of mechanisms, including chemical bonding, van der Waals interactions, and solvation effects. The strong coupling between the molecule and the plasmonic structure leads to the formation of a plasmonic-molecule hybrid state, which can be excited by light and emit radiation.

The observed enhancement in radiative emission from the plasmonic system can be attributed to the molecule’s ability to increase the local field strength at the plasmonic surface. This enhancement can lead to a significant increase in the efficiency of energy transfer from the molecule to the plasmonic system, and can be used to enhance the emission from plasmonic nanostructures.

The molecule-induced effect has a number of potential applications, including the development of new plasmonic sensors and detectors, the enhancement of the emission from plasmonic nanostructures, and the creation of new plasmonic materials.

References:

23. The fact the molecule-induced effect dominates can be seen by comparing Figs. 4(a) and 4(d) of Ref. 12, which show that the effective temperature of the electronic Raman continuum in a molecular junction that carries a current of ∼2 mA exceeds that of a bare junction with ten times larger current.
31. Considerations of coupling magnitudes imply that energy transfer from individual electron-hole pair excitations is an unlikely event. This does not preclude the notion that radiative emission from those electron-hole pairs that couple to the plasmon (those generated by radiationless decay of the plasmon) is enhanced relative to other e-h pairs. The bottom line agrees with the observations of Refs. 112 and 113: Emission is enhanced at the plasmon frequency range.